

A uniform horizontal beam 5.00 m long and weighing  $3.00 \times 10^2 \text{ N}$  is attached to a wall by a pin connection that allows the beam to rotate. Its far end is supported by a cable that makes an angle of  $53.0^\circ$  with the horizontal. If a person weighing  $6.00 \times 10^2 \text{ N}$  stands 1.50 m from the wall, find the magnitude of the tension in the cable and the force exerted by the wall.

$\tau = F \cdot d$

$\Sigma \tau = 0$

$\tau_1 - \tau_2 - \tau_3 = 0$

$T_y(5) - F_{g1}(2.5) - F_{g2}(1.5) = 0$

$T_y = \frac{F_{g1}(2.5) + F_{g2}(1.5)}{5}$

$T_y = \frac{300(2.5) + 600(1.5)}{5}$

$T_y = 330 \text{ N}$

$\Sigma F_x = 0$

$T_y + F_{wy} - F_{g1} - F_{g2} = 0$

$F_{wy} = F_{g1} + F_{g2} - T_y$

$F_{wy} = 300 + 600 - 330$

$F_{wy} = 570 \text{ N}$

$\Sigma F_x = 0$

$-T_x + F_{wx} = 0$

$F_{wx} = T_x$

$F_{wx} = T \cos \theta$

$F_{wx} = 415 \cos 53$

$F_{wx} = 249 \text{ N}$

$\Sigma \tau = 0$

$-\tau_1 + \tau_2 + \tau_3 = 0$

$-F_{wy}(5) + F_{g1}(3.5) + F_{g2}(2.5) = 0$

$a^2 + b^2 = c^2$

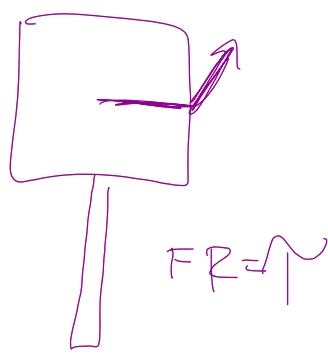
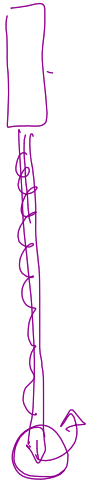
$c = 622 \text{ N}$

$66.4^\circ \text{ N of E}$

$H = 413 \text{ N}$

1 Using a screwdriver, you try to remove a screw from a piece of furniture, but can't get it to turn. To increase the chances of success you should use a screwdriver that

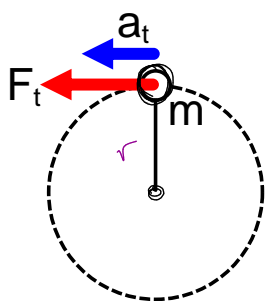
- A is longer
- B is shorter
- C has a narrower handle
- D has a wider handle



2 A constant net torque is applied to an object. Which one of the following will not be constant?

- A angular acceleration
- B angular velocity
- C moment of inertia
- D center of gravity

## Torque and Angular Acceleration



$$F_t = ma_t$$

$$F_t r = ma_t r$$

$$\tau = m a_t r$$

$$a_t = \alpha r$$

$$\tau = m \alpha r^2$$

Force  $\tau = m r^2 \alpha$  accel

↑

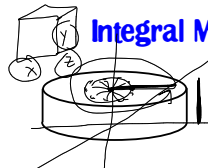
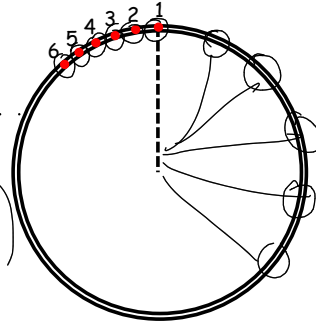
Moment of Inertia

$$I = \sum mr^2$$

$$I = M_1 r_1^2 + M_2 r_2^2 + M_3 r_3^2 + \dots$$

$$I = r^2 (M_1 + M_2 + M_3 + \dots)$$

$$I = Mr^2$$



**Integral Moments of Inertia**

$$\int r^2 dm$$

small piece

$$\int_0^h \left[ \int_0^{2\pi} \left[ \int_0^R r^2 \rho r dr d\theta dz \right] \right]$$

$$\rho = \frac{M}{V}$$

$$M = \rho V \text{ const}$$

$$dm = \rho dV$$

$$dV = r dr d\theta dz$$

$$dm = \rho r dr d\theta dz$$

$$\int_0^h \int_0^{2\pi} \left[ \int_0^R \rho r^3 dr d\theta dz \right]$$

$$\int_0^h \int_0^{2\pi} \frac{1}{4} R^4 \rho d\theta dz$$

$$\int_0^h \frac{1}{4} R^4 \rho \int_0^{2\pi} d\theta dz$$

$$\int_0^h \frac{1}{4} R^4 \rho 2\pi dz$$

$$\frac{1}{4} R^4 \rho 2\pi z \Big|_0^h$$

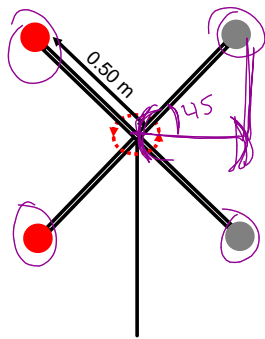
$$I = \frac{1}{4} R^4 \rho 2\pi h \quad \rho = \frac{M}{V}$$

$$= \frac{1}{4} R^4 \frac{M}{\pi R^2 h} = \frac{1}{4} R^2 M$$

$$= \frac{1}{2} R^2 M$$

- -0.30 kg
- -0.20 kg

What is the Moment of Inertia for the object below?



$$I = \sum Mr^2$$

$$I = m_1 r_1^2 + m_2 r_2^2 + m_3 r_3^2 + m_4 r_4^2$$

$$I = r^2 (m_1 + m_2 + m_3 + m_4)$$

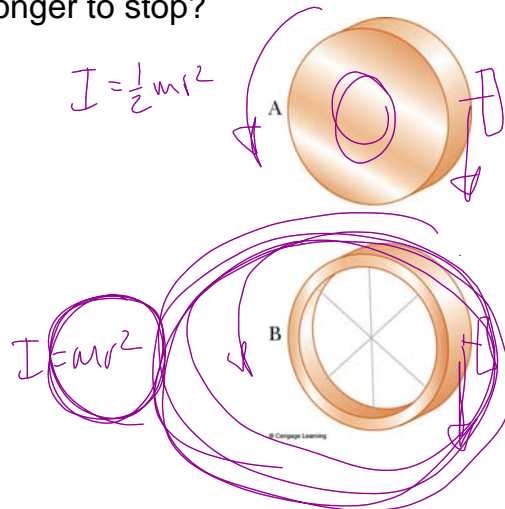
$$I = r^2 = (0.50 \cos 45)^2$$

$$I = 0.123 \text{ kgm}^2$$

3 Two rigid objects shown have the same mass, radius, and angular speed. If the same braking torque is applied to each, which takes longer to stop?

- A A
- B B
- C Have No Clue

~~B = same~~



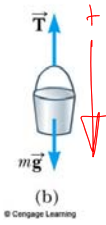


A solid frictionless cylindrical reel of mass  $M=3.00$  kg and radius  $R=0.400$  m is used to draw water from a well. A bucket of mass  $m=2.00$  kg is attached to a cord that is wrapped around the cylinder.

- (a) Find the tension  $T$  in the cord and acceleration  $a$  of the bucket.
- (b) If the bucket starts from rest at the top of the well and falls for 3.00 s before hitting the water, how far does it fall?

(a)

$I = \text{moment of inertia}$

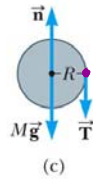


(b)

Bucket

$$\sum F = ma$$

$$mg - T = m\overset{?}{a}$$



(c)

$$\sum \tau = I\alpha$$

$$\sum \tau = \frac{1}{2}mr^2\alpha$$

$$TR = \frac{1}{2}mr^2\overset{?}{\alpha}$$

$$TR = \frac{1}{2}mr^2 \frac{a_T}{r}$$

$$a_T = \alpha r$$

$$\alpha = \frac{a_T}{r}$$